

Reading assignment: sections 21.1-21.3 of the **NEW** text.

Problem 1. In the Bizarro Universe, long ago and very far away, scientists have determined that everything is just like in our universe except that electrons are fermions with spin 3/2 instead of spin 1/2. Consider atomic states for Bizarro electrons.

- (a) How many Bizarro electrons can fit into each  $s$  ( $l = 0$ ) orbital? How many Bizarro electrons can fit into each  $p$  ( $l = 1$ ) orbital?
- (b) What are the atomic numbers of the lightest two Bizarro noble gases (the lightest has a filled  $1s$  orbital, the next has a filled  $2p$  orbital)?
- (c) Consider Bizarro neon, by which we mean a neutral atom with  $Z = 10$ . What is the electron configuration, instead of  $(1s)^2(2s)^2(2p)^6$  as in our universe? Will it behave chemically like a noble gas? What are all of the  $^{2S+1}L_J$  spectroscopic terms for the electron configuration you found, and which of them is the ground state?

Problem 2. In class and in the text, we evaluated the probability that a  ${}^3\text{H}$  (tritium) atom in its ground state would end up in the ground state of  ${}^3\text{He}$ , after beta decay, and found  $P = 512/729$ . In the same way, evaluate the probability that the atom ends up in each of the  $n = 2$  or  $n = 3$  levels instead. Check that the total probability for ending up in the  $n = 1$ ,  $n = 2$ , and  $n = 3$  levels does not exceed 1.

Problem 3. A particle of mass  $m$  moves freely in a 1-dimensional box of length  $a$ , with the left edge at  $x = 0$  and the right edge at  $x = a$ . At time  $t = 0$ , the particle is in the ground state, and the box is suddenly lengthened by expanding the right edge out to  $x = b$ .

- (a) Find the probability that the particle ends up in *each* of the energy eigenstates of the final box, labeled by positive integers  $n$ . (Make sure that your probabilities are dimensionless.)
- (b) Use your results from part (a), and your knowledge of the laws of probability, to evaluate the following mathematical infinite sum over  $n$ :

$$S(a, b) = \sum_{n=1}^{\infty} \frac{\sin^2(n\pi a/b)}{(n^2 a^2 - b^2)^2}.$$

Quantum mechanics knows how to do non-trivial sums!

- (c) As a check, for the special case  $b = 2a$ , evaluate the individual probabilities numerically for each integer up to  $n = 10$ , and their total with 6 significant digits. (Be careful for  $n = 2$ ; the answer is non-zero and finite.)