

Evaluate the following limits

1.
$$\lim_{x \rightarrow 4} \frac{x^2 - 4x}{x^2 - 3x - 4}$$

(a) Try plugging in $x = 4$ to see what happens.

$$\lim_{x \rightarrow 4} \frac{x^2 - 4x}{x^2 - 3x - 4} = \frac{(4)^2 - 4(4)}{(4)^2 - 3(4) - 4} = \frac{0}{0}$$

(b) This is called an indeterminate. It means we can't get the value by just plugging in it. The limit might exist or it might not. We must use a different method. We work around this by factoring the top and bottom.

(c) Factor the top and bottom

$$\begin{aligned} \lim_{x \rightarrow 4} \frac{x^2 - 4x}{x^2 - 3x - 4} &= \lim_{x \rightarrow 4} \frac{x(x - 4)}{(x - 4)(x + 1)} \\ &= \lim_{x \rightarrow 4} \frac{x}{x + 1} \\ &= \frac{4}{5} \end{aligned}$$

2.
$$\lim_{x \rightarrow 0} \frac{x}{3x^2 + x}$$

(a) Try plugging in $x = 0$ to see what happens.

$$\lim_{x \rightarrow 0} \frac{x}{3x^2 + x} = \frac{0}{3(0)^2 + 0} = \frac{0}{0}$$

(b) This is called an indeterminate. It means we can't get the value by just plugging in it. The limit might exist or it might not. We must use a different method. We work around this by factoring the top and bottom.

(c) Factor the top and bottom

$$\begin{aligned}
\lim_{x \rightarrow 0} \frac{x}{3x^2 + x} &= \lim_{x \rightarrow 0} \frac{x}{x(3x + 1)} \\
&= \lim_{x \rightarrow 0} \frac{1}{3x + 1} \\
&= \frac{1}{3(0) + 1} \\
&= 1
\end{aligned}$$

3. $\lim_{x \rightarrow -5} \frac{3x^2 + 22x + 35}{2x^2 + 9x - 5}$

(a) Try plugging in $x = -5$ to see what happens.

$$\lim_{x \rightarrow -5} \frac{3x^2 + 22x + 35}{2x^2 + 9x - 5} = \frac{3(-5)^2 + 22(-5) + 35}{2(-5)^2 + 9(-5) - 5} = \frac{0}{0}$$

(b) This is called an indeterminate. It means we can't get the value by just plugging in it. The limit might exist or it might not. We must use a different method. We work around this by factoring the top and bottom.

(c) Factor the top and bottom

$$\begin{aligned}
\lim_{x \rightarrow -5} \frac{3x^2 + 22x + 35}{2x^2 + 9x - 5} &= \lim_{x \rightarrow -5} \frac{(x + 5)(3x + 7)}{(x + 5)(2x - 1)} \\
&= \lim_{x \rightarrow -5} \frac{3x + 7}{2x - 1} \\
&= \frac{3(-5) + 7}{2(-5) - 1} \\
&= \frac{8}{11}
\end{aligned}$$