

Reading assignment: Griffiths pages 1-24, and the 5 page “Advertisement” just before Chapter 1.

Problem 1 Compute the dot product and the cross product of the constant vectors:

$$\begin{aligned}\vec{\mathbf{A}} &= 2\hat{x} - 7\hat{y} + 3\hat{z} \\ \vec{\mathbf{B}} &= 4\hat{x} + \hat{y} - 2\hat{z}\end{aligned}$$

What is the angle between the vectors $\vec{\mathbf{A}}$ and $\vec{\mathbf{B}}$?

Problem 2 Find the gradients of the functions:

- (a) $f(x, y, z) = xy^3z$
- (b) $f(x, y, z) = \sqrt{x^2 + y^2 + z^2}$
- (c) $f(x, y, z) = e^z \cos(y)$

Problem 3 Find the divergence and the curl of the vector function:

$$\vec{\mathbf{B}}(x, y, z) = (x^2 + yz)\hat{x} + (y^2 + zx)\hat{y} + (z^2 + xy)\hat{z}$$

Problem 4 Prove by explicit calculation that the divergence of the curl of *every* vector field $\vec{\mathbf{A}}(x, y, z)$ is always zero.

Problem 5 Find the Laplacian of each of the functions in Problem 2.